**Problem 4.4** If the stable isotope of sodium is <sup>23</sup>Na, what kind of radioactivity would you expect from (a) <sup>22</sup>Na and (b) <sup>24</sup>Na?

We know that  $^{23}$ Na $^{11}$  is stable. The isotope  $^{22}$ Na $^{11}$  has one less neutron, while  $^{24}$ Na $^{11}$  has one extra neutron relative to  $^{23}$ Na $^{11}$ . Consequently, a proton in  $^{22}$ Na $^{11}$  can undergo an inverse  $\beta$  decay to yield

$$^{22}\text{Na}^{11} \rightarrow ^{22}\text{Ne}^{10} + e^+ + \nu_e,$$
 (4.37)

where  $^{22}{\rm Ne^{10}}$  is a naturally occurring stable isotope of  $^{20}{\rm Ne^{10}}$ . Similarly, the extra neutron in  $^{24}{\rm Na^{11}}$  can undergo a  $\beta$  decay to yield

$$^{24}\text{Na}^{11} \to ^{24}\text{Mg}^{12} + e^- + \bar{\nu}_e,$$
 (4.38)

where  $^{24}$ Mg $^{12}$  is stable.